# **Transformation toughening**

**Part 4** *Fabrication, fracture toughness and strength of AI203 - Zr02 composites* 

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Three AI<sub>2</sub>O<sub>3</sub>-ZrO<sub>2</sub> composite series, containing 0, 2 and 7.5 mol %  $Y_2O_3$ , were fabricated for fracture toughness determinations. Without  $Y_2O_3$  additions, tetragonal-phase  $ZrO<sub>2</sub>$  could only be retained up to approximately 10 vol %  $ZrO<sub>2</sub>$ ; additions of 2 mol %  $Y_2O_3$  allowed full retention of the tetragonal phase up to 60 vol % ZrO<sub>2</sub>. Cubic ZrO<sub>2</sub> was produced with additions of 7.5 mol %  $Y_2O_3$ . Significant toughening and strengthening was achieved when tetragonal  $ZrO<sub>2</sub>$  was present.

# **1. Introduction**

In Part 1 [1] of this series of papers, the thermodynamics of a constrained phase transformation was presented, with particular reference to the size-effect associated with retention of the high temperature phase. Part 2 [2] presented the theory concerning the contribution of the stressinduced transformation to fracture toughness. Part 3 [3] reported experimental observations concerning the retention of tetragonal-phase  $Z<sub>r</sub>O<sub>2</sub>$ and its contribution to fracture toughness for a series of materials fabricated in the  $ZrO<sub>2</sub>-Y<sub>2</sub>O<sub>3</sub>$ system. The theory shows that both the critical inclusion size and the contribution to fracture toughness can be increased by choosing a constraining matrix with an elastic modulus higher than that of  $ZrO<sub>2</sub>$ .

The  $Al_2O_3 - ZrO_2$  system was chosen for this study because  $Al_2O_3$  has approximately twice the elastic modulus of  $ZrO<sub>2</sub>$  (390 compared with 207 GPa) and both phases are chemically compatible with one another [4]. Claussen [5] has already demonstrated that  $Al_2O_3 - ZrO_2$  polycrystalline composites could be fabricated, and he also has demonstrated [6] that tetragonalphase  $ZrO<sub>2</sub>$  could be retained in volume-fractions up to 0.17. The intent of the present work was to fabricate a series of  $Al_2O_3 - ZrO_2$  composite materials from one end-member to the other and

to retain the  $ZrO<sub>2</sub>$  in its tetragonal state. Initial studies indicated that, within the range of fabrication parameters investigated, "pure" tetragonal  $ZrO<sub>2</sub>$  could only be retained in volume-fractions less than 0.10. Based on theoretical considerations (from Part 1 [1]) and retention studies in the  $ZrO<sub>2</sub>-Y<sub>2</sub>O<sub>3</sub>$  system (Part 3 [3]), it was found that additions of 2 mol%  $Y_2O_3$  to the composite powders would allow the retention of the tetragonal phase to much greater volume-fractions of ZrO2. Thus, this series of materials formed the principal base for investigating the contribution of the stress-induced phase transformation to fracture toughness and strength.

# **2. Experimental procedure**

### 2.1. Fabrication and phase identification

Three  $\text{Al}_2\text{O}_3-\text{ZrO}_2$  composite series were fabricated for this study: one containing  $ZrO<sub>2</sub>$  volumefractions of up to 0.20, one containing  $ZrO<sub>2</sub>$  + 2 mol%  $Y_2O_3$  in which tetragonal-phase  $ZrO_2$  was retained, and one containing  $ZrO<sub>2</sub> + 7.5$  mol%  $Y_2O_3$  in which cubic  $ZrO_2$  was obtained. The latter composite series was used for base-line information where transformation toughening was not a phenomena associated with the fracture mechanics of the material.

Powders with sub-micrometre particle size were used\*.  $Y_2O_3$  was introduced as soluble yttrium

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 $*$ A1<sub>2</sub>O<sub>3</sub> from Lindy B, Union Carbide Corp.; ZrO<sub>2</sub> from Zircar Corp.

nitrate\*. Composite powders were mixed by ballmilling with methanol and  $Al_2O_3$  balls in a plastic container. All powders were dried; those containing yttrium nitrate were calcined at  $400^{\circ}$ C for 4h. Densification was achieved by hot-pressing. Most  $Y_2O_3$ -containing compositions were hotpressed at  $1600^{\circ}$ C for 2h; compositions containing 80 and 100 vol %  $ZrO<sub>2</sub>$  (plus 2 mol %  $Y<sub>2</sub>O<sub>3</sub>$ ) were hot-pressed at  $1400^{\circ}$  C in order to achieve a smaller grain size which would allow the retention of the tetragonal-phase  $ZrO<sub>2</sub>$ . The non-yttria composites were hot-pressed at  $1500^{\circ}$  C, for the purpose, again, of achieving a smaller grain size in order to optimize the retention of tetragonal-phase  $ZrO<sub>2</sub>$ . The pure  $Al<sub>2</sub>O<sub>3</sub>$  end-member was hotpressed at  $1400^{\circ}$  C to achieve a grain size comparable with the two-phase materials (the introduction of one end-member into the other limited grain growth).

Archimedes' technique was used to measure the density of the 5 cm diameter billets. Specimens were cut, ground and polished<sup>†</sup> prior to phase identification by X-ray diffraction analysis.  $2\theta$ -scans between 27 and 33 $^{\circ}$  were used to estimate the tetragonal/monoclinic  $ZrO<sub>2</sub>$  ratio;  $2\theta$ scans between 55 and  $62^\circ$  were used to confirm either the tetragonal or the cubic  $ZrO<sub>2</sub>$  phase.

### **2.2. Mechanical** measurement

Young's modulus,  $E$ , of selected compositions was measured at room temperature by the resonance technique with two modes of vibration: flexural (9 k Hz) and extensional (60 kHz).

The critical stress-intensity factor,  $K_c$ , was measured on polished specimens using the identation technique (20 kg load) developed by Evans and Charles  $[7]$ . Hardness,  $H$ , data was also obtained. Three measurements were made for each material.

Flexural strength measurements were obtained in four-point bend testing (inner span: 1.22 cm; outer span: 2.54 cm) on diamond-cut specimens (of cross-section approximately  $0.32 \text{ cm} \times 0.32 \text{ cm}$ finished with a 220 grit diamond grinding wheel.

# **3. Results**

### 3.1. Fabrication and phase identification

Table I lists the fabrication conditions for the compositions reported here and their respective average properties. In the series which excluded  $Y_2O_3$ , high proportions of the tetragonal-phase  $ZrO<sub>2</sub>$  could only be retained up to approximately 10 vol%  $ZrO<sub>2</sub>$ . In the series containing 2 mol%  $Y_2O_3$ , tetragonal-phase  $ZrO_2$  was fully retained up to about 60 vol%  $ZrO_2$ . Cubic  $ZrO_2$  was the only  $ZrO<sub>2</sub>$  structure observed in the series containing 7.5 mol%  $Y_2O_3$ . No Y-Al oxide compounds were observed.

Lattice-parameter measurements reported by Scott [8] are confirmed in the present work:  $a = 0.5090$  nm,  $c = 0.5174$  nm for the tetragonal (plus  $2 \text{ mol } \% Y_2O_3$ ) structure and  $a = 0.5135 \text{ nm}$ for the cubic structure. Using these values and the formulation  $Zr_{1-x}Y_xO_{2-(x/2)}$ , the theoretical densities for the tetragonal and cubic structures were calculated as  $6.09$  and  $5.97 \text{ cm}^{-3}$ , respectively. Measured densities,  $\rho$ , for the two composite series containing either the tetragonal or the cubic phases obeyed the Rule of Mixtures for the endmembers  $(Al_2O_3: \rho = 3.98 \text{ g cm}^{-3})$ , indicating that theoretical density was achieved during fabrication.

Fig. 1 illustrates microstructures of the polished surfaces typical of the  $Al_2O_3 - ZrO_2$  composites (cracks present were purposely propagated from hardness indents). The observed agglomeration of the minor phase in occasional groups of 2 to 5 grains indicates that the dispersion could be improved. The average  $ZrO<sub>2</sub>$  grain-size, d, for the composite materials was dependent on the fabrication temperature:  $d \sim 0.2 \mu m$  at 1400°C,  $d \sim 0.5$  µm at 1500°C and  $d \sim 1$  µm at 1600°C. The average grain-size for the single-phase endmembers was approximately  $2 \mu m$  for  $Al_2O_3$ and approximately 0.5  $\mu$ m for ZrO<sub>2</sub>.

As reported in the Appendix, hot-pressed billets containing greater than 30 vol %  $Al_2O_3$ contained large surface cracks, as observed by fluorescent-dye penetration. Although small crackfree specimens could be cut and polished for  $K<sub>e</sub>$ measurements, larger bar specimens invariably contained one or more cracks, which restricted meaningful strength measurements to composites containing  $\leq 30$  vol % ZrO<sub>2</sub>.

### **3.2.** Hardness

Fig. 2 illustrates the Vickers hardness (20 kg) for the  $Al_2O_3 - ZrO_2$  (plus 2 mol%  $Y_2O_3$ ) series,

\*Research Chemicals Inc.

]'Surface damage caused by cutting and grinding causes the surface to transform. Polishing decreases the depth of the transformed surface layer.

ZrO <sub>2</sub> content $(vol\%)$	$Y_2O_3$ content $(mod \%)$	Fabrication conditions		Density $(gm cm^{-3})$	Volume-fraction $ZrO2 phase*$	Hardness, $H$ (GPa)	Young's modulus, $E$	$K_{\rm c}$ $(MPa m^{1/2})$
		Temperature (°C)	Time (h)		$(\%)$		(GPa)	
		$Al_2O_3 - ZrO_2$ (plus 2 mol% $Y_2O_3$ ) series						
0		1400	2	3.98		17.6	390	4.89
6	$\mathbf{2}$	1600	$\overline{c}$	4.12	100t	16.8		5.97
12.3	$\overline{2}$	1600	$\overline{\mathbf{c}}$	4.26	100t	15.9		6.22
18.2	$\overline{c}$	1600	$\overline{c}$	4.38	100t	16.1	356	6.58
23.9	$\mathbf{2}$	1600	$\overline{c}$	4.50	100t	16.4		6.38
29.5	$\overline{c}$	1600	$\overline{\mathbf{c}}$	4.62	100t	15.7	<b></b>	7.43
45.0	$\overline{c}$	1600	$\overline{c}$	4.89	$tr-m$	15.1	291	8.12
60.0	$\overline{c}$	1600	$\overline{c}$	5.24	$\sim$ 95t	13.7	-	7.45
80.0	$\overline{2}$	1400	$\overline{c}$	5.57	$\sim 85t$	12.6	237	6.79
100.0	$\mathbf{2}$	1400	$\overline{2}$	6.01	$\sim 80t$	11.6	210	6.62
	$\text{Al}_2\text{O}_3 - \text{ZrO}_2$ (pure) series							
7.5		1500	$\mathfrak{p}$	4.12	$\sim$ 90t	17.2		5.88
10.0		1500	$\overline{2}$	4.15	$\sim 80t$	15.8		6.73
12.5		1500	$\boldsymbol{2}$	4.22	$\sim$ 70t	16.9		6.21
15.0		1500	$\overline{c}$	4.25	$\sim 50t$	17.3		5.71
20.0		1600	$\overline{c}$		< 20t	10.1		(5.25)
		$\text{Al}_2\text{O}_3 - \text{ZrO}_2$ (plus 7.5 mol% $\text{Y}_2\text{O}_3$ ) series						
20.0	7.5	1600	2	4.46	100c	15.8		4.54
40.0	7.5	1600	2	4.89	100c	15.9		3.75
60.0	7.5	1600	$\mathbf{2}$	5.28	100c	15.0		3.50
80.0	7.5	1600	$\boldsymbol{2}$	5.63	100c	14.3		3.14
100.0	7.5	1600	$\boldsymbol{2}$	5.95	100c	11.4		3.90

TABLE I Fabrication conditions, phase content and properties of  $A1_2O_3-ZrO_2$  composites

\* $t =$  tetragonal; c = cubic; tr-m = trace monoclinic.

suggesting that the hardness obeys a linear Rule of Mixtures. The 20 vol%  $ZrO<sub>2</sub>$  (pure) composition had an exceptionally low hardness (see Table I), Its high monoclinic-phase content and friable nature suggested that it contained a high density of microcracks. Scanning electron microscope observations adjacent to the hardness indent in this material indicated that the indenter pushed the microcracked material aside as it extended.

### 3.3. Young's modulus

Fig. 3 reports the Young's modulus values of the  $Al_2O_3 - ZrO_2$  (plus 2 mol%  $Y_2O_3$ ) series obtained from the two resonance techniques.

### **3.4. Critical stress-intensity factor**

Fig. 4a reports  $K_{\rm c}$  as a function of composition for the two series containing  $Y_2O_3$ . A considerable increase in fracture toughness could be achieved with the addition of the tetragonal-phase  $ZrO<sub>2</sub>$ (series containing 2 mol  $\%\ Y_2O_3$ ). In contrast, the addition of cubic-phase  $ZrO<sub>2</sub>$  lowered the fracture toughness (the series containing 7.5 mol  $\%\text{Y}_2\text{O}_3$ ). Fig. 4b shows that the peak in  $K_c$  for the series that excluded  $Y_2O_3$  corresponds to the maximum retention of the tetragonal phase in this series.

### 3.5. Strength

Flexural-strength determinations for the series containing  $2 \text{ mol } \%$  Y<sub>2</sub>O<sub>3</sub> are shown in Fig. 5.Since it is known that surface grinding can result in compressive surface stresses in these types of materials, a set of specimens were annealed at  $1300^{\circ}$  C prior to testing to eliminate the transformed surface-layer. Annealing resulted in a lower average strength. It is interesting to note that significant strengthening of  $Al_2O_3$  can be achieved by adding the tetragonal-phase  $ZrO<sub>2</sub>$  toughening agent.

## **4. Discussion**

## **4.1. Retention of** tetragonal ZrO:

Part 1 [1] of this series of papers showed that the critical grain-size for retention of the hightemperature tetragonal structure of  $ZrO<sub>2</sub>$  could be increased by increasing the elastic modulus of the constraining matrix and by alloying to decrease



*Figure 1* SEM micrographs of polished surfaces of A1<sub>2</sub>O<sub>3</sub>-ZrO<sub>2</sub> (plus 2 mo1% Y<sub>2</sub>O<sub>3</sub>) composites at ZrO<sub>2</sub> volumefractions of (a) 0.063, (b) 0.123, (c) 0.45 and (d) 0.80.  $Al_2O_3$  is dark-phase.

the chemical free-energy change. Data presented here are consistent with these theoretical conclusions. Namely, without  $Y_2O_3$  additions, retention of tetragonal  $ZrO<sub>2</sub>$  became increasingly more difficult as the elastic modulus of the composite decreased. Additions of 2 mol  $\%$  Y<sub>2</sub>O<sub>3</sub> resulted in tetragonal-phase retention to much larger  $ZrO<sub>2</sub>$ volume-fractions, despite the decreased modulus and larger grain-size. Part 3 [3] of this series of papers showed that the critical grain-size for  $ZrO<sub>2</sub>$ (plus  $2 \text{ mol } \%\ Y_2O_3$ ) was approximately  $0.2 \mu \text{m}$ when the constraining matrix was  $ZrO<sub>2</sub>$ . The current study shows that the critical grain-size can be increased to at least  $1 \mu m$  with the higher modulus of the  $Al_2O_3 - ZrO_2$  constraining matrix. In addition, as the composition approached the  $ZrO<sub>2</sub>$  end-member, the fraction of tetragonalphase retained decreased.

#### 4.2. Fracture toughness

Fracture-toughness data presented in Fig. 4 clearly illustrate that the tetragonal-phase is the toughening agent. When cubic  $ZrO<sub>2</sub>$  is incorporated into  $Al_2O_3$ , the toughness decreases. This may be a result of residual stresses associated with differential thermal expansion. Data for the series which excluded  $Y_2O_3$  indicate that the toughness decreased with increasing monoclinic content.

Part 2 [2] of this series presented an expression for  $K_c$ :



Figure 2 Vicker's hardness (measured at 20 kg) for the  $Al_2O_3 - ZrO_2$  (plus 2 mol% **Y~O 3) composite series.** 

$$
K_c = \begin{bmatrix} K\bar{0} + \frac{1}{(1 - \nu_c^2)} \end{bmatrix},
$$
  
(1)  
where  $K_0$  is the critical stress-intensity factor for

the composite without the transformation toughening phenomena,  $(|\Delta G^c| - \Delta U_{\rm se} f)$  is the work done per unit volume to stress-induce the transformation,  $E_c$  and  $v_c$  are the elastic properties of the

composite,  $V_i$  is the volume-fraction of the tetragonal-phase  $ZrO<sub>2</sub>$  and R is the size of the transformation-zone adjacent to the crack. By using the measured values of  $K_c$  for the series containing the tetragonal-phase  $ZrO<sub>2</sub>$ , the values of  $K<sub>0</sub>$  obtained from the series containing cubic-phase  $ZrO<sub>2</sub>$ , the  $E_c$  value from Fig. 3,  $v_c = 0.25$  and assuming that  $R = 1 \mu m$  (i.e., the average grain-size for this series when  $V_i \le 60$  vol%  $ZrO_2$ ), the average value of



*Figure 3* Young's modulus plotted 1.0 against composition for the  $Al_2O_3 -$ <br>  $ZrO_2$   $ZrO_6$  (plus 2 mol% Y, O, ) series.  $ZrO<sub>2</sub>$  (plus 2 mol%  $Y<sub>2</sub>O<sub>3</sub>$ ) series.



 $(|\Delta G^c| - \Delta U_{\rm se} f)$  was calculated as 188 MJ m<sup>-3</sup> for compositions containing less than  $60$  vol% tetragonal-phase  $ZrO<sub>2</sub>$ . The agreement of the experimental data with this value is shown by the solid line drawn through the  $Al_2O_3 - ZrO_2$  (tetragonal-phase) data. Although this value is in good agreement with that calculated in Part 3 for the  $ZrO<sub>2</sub> + 3 mol\%$  Y<sub>2</sub>O<sub>3</sub> material (188 compared with  $176 \text{ MJ m}^{-3}$ ), this agreement may be fortuitous since the magnitude of the terms in  $(|\Delta G^c| - \Delta U_{\rm se} f)$  are expected to be different for the two systems. Namely,  $|\Delta G^c|$  should be greater for the  $ZrO_2 + 2$  mol%  $Y_2O_3$  composition relative to the  $ZrO_2 + 3$  mol %  $Y_2O_3$  composition, and  $\Delta U_{\rm se}$  should be greater for the higher modulus  $Al_2O_3 - ZrO_2$  constraining matrix relative to constraint with  $ZrO<sub>2</sub>$  alone.

As shown in Fig. 4a, good agreement between theory (Equation 1) and the experimental data is obtained for compositions containing  $\leq 0.45$  vol %  $ZrO<sub>2</sub>$ . Poor agreement is obtained at higher volume-fractions. This lack of agreement may be due to the lack of total retention of the tetragonalphase  $ZrO_2$  when  $V_i$  is greater than 60 vol%, the



*Figure 4* (a) Critical stress-intensity factor plotted against composition for the  $Al_2O_3-ZrO_2$  (plus 2 mol%  $Y_2O_3$ ) (tetragonal) and the  $AI_2O_3$ -ZrO<sub>2</sub> (plus 7.5 mol%  $Y_2O_3$ ) (cubic) series. (b) Critical stress-intensity factor plotted against composition for the  $Al_2O_3 - ZrO_2$  (pure) series.

smaller grain-size of the higher  $ZrO_2$ -content compositions and/or a compositional difference due to the apparent oxygen deficiency of the  $ZrO<sub>2</sub>$  phase (see the Appendix).

#### 4.3. Strength

The strength data presented in Fig. 5 have been analysed to determine their dependence on the experimental  $K<sub>c</sub>$  values. In this analysis, it was assumed that the crack-size distribution responsible for failure remained unchanged from material to material. With this assumption, the strength of each material should be related to that of any other by a relation that is dependent of their respective critical stress-intensity factor such that

$$
\sigma_2 = \frac{K_2}{K_1} \sigma_1, \qquad (2)
$$

where  $\sigma_1$  and  $\sigma_2$  and the strengths of any two materials and  $K_1$  and  $K_2$  are their respective critical stress-intensity factors. This relation was used, with the average strength and  $K_c$  values for the pure  $Al_2O_3$ , to obtain the broken line in Fig. 5. As shown, three of the five original sets of data were in good agreement with this



*Figure 5* Flexural strength plotted against composition for the A1<sub>2</sub>O<sub>3</sub>-ZrO<sub>2</sub> (plus 2 mol % Y<sub>2</sub>O<sub>3</sub>) series.

analysis; however, two of the data sets  $(V_i =$ 0.182 and 0.295) were higher than predicted.

Pascoe and Garvie [9] have shown that surface compressive stress arises in materials containing metastable tetragonal  $ZrO<sub>2</sub>$  when the transformation at the surface is induced by an abrasion process. The volume increase associated with the transformed surface-layer gives rise to the compressive stresses. Since each set of specimens was independently surface ground it was suspected that several of these sets (the two that resulted in the higher values) may have received sufficient surface damage to impart enough surface compressive stress to increase their strength. To test this hypothesis, the effect of surface abrasion on strength was examined. Although the principal results of this work will be reported elsewhere [10], it was shown that when the abrasivelyground specimens were annealed at  $1300^{\circ}$ C to eliminate the transformed surface layer, the average strength was lowered to that expected from Equation 2. These data are shown by the open triangle in Fig. 5.

It can be concluded that the strength of the  $Al_2O_3 - ZrO_2$  (plus 2 mol%  $Y_2O_3$ ) composite materials increases in a way proportional to their increase in  $K_c$  values, as expected. Additional strengthening can be obtained by compressive stressing the surfaces through abrasion. Studies are currently underway to characterize and optimize the abrasion phenomena.

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# **Appendix:** Formation of surface cracks during the hot-pressing of  $Al_2O_3 - ZrO_2$ composites

As indicated in the text,  $Al_2O_3 - ZrO_2$  composites containing greater than 30 vol%  $ZrO<sub>2</sub>$  hotpressed in graphite dies were observed to contain large surface cracks. Although the exact cause of the stresses that give rise to these cracks is beyond the scope of the present work, the experimental observations indicate a probable cause.

The colour of hot-pressed  $Al_2O_3 - ZrO_2$  composite billets changes from a light grey to black as the  $ZrO<sub>2</sub>$  volume-fraction increased to 1. A colour gradient also exists within a sectioned billet, darker on the outside, lighter near the centre. This colour gradient indicates a compositional gradient. Black  $ZrO<sub>2</sub>$  can also be produced at high temperatures in vacuum and  $ZrO<sub>2</sub>$  is known to lose oxygen in high-temperature lowoxygen content environments. [ 11 ].

X-ray diffraction examination did not reveal phases other than the  $ZrO<sub>2</sub>$  structures indicated in the text (Table I). Surface and interior phases were the same (precise lattice-parameter measurements were not performed).

Oxidation in air at  $1300^{\circ}$ C transformed the grey-to-black specimens to pure white. Specimens oxidized for short periods revealed, when sectioned, a dark core. Oxidation resulted in moderate to severe surface spalling for compositions containing greater than 30 vol %  $ZrO<sub>2</sub>$ . The 100 vol %  $ZrO<sub>2</sub>$  specimens could be completely oxidized in 15 min at  $750^{\circ}$  C due to severe cracking.

The above evidence suggests that the dark colour is consistent with an oxygen-difficient  $ZrO<sub>2</sub>$ -phase. Ruh and Garrett [12] have shown that the oxygen-difficient  $ZrO<sub>2</sub>$  has a smaller molar volume. Thus, a gradient in the oxygencontent of the  $ZrO<sub>2</sub>$ -phase from the billet surface to its interior would result in surface tensile stresses at the fabrication temperature. With a sufficient volume-fraction of  $ZrO<sub>2</sub>$  (e.g.,

**> 30 vol%), these tensile stresses could be significant enough to produce surface cracks. Similarly, oxidation would increase the molar volume of the depleted phase to produce surface compressive stresses and surface spalling [ 12].** 

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